



CS3701 - Operating Systems

Chapter 6 - Deadlocks

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1.1 Overview

1.2 System Model

1.3 Deadlock Characterization

2. Resource-Allocation Graph

2.1 RAG Components

2.2 RAG Deadlock Analysis - Basic Facts

2.3 RAG Examples Analysis

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Outline (Contd.)

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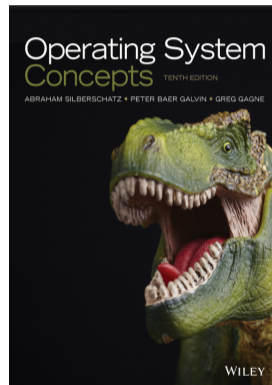
7. Exercise

Textbook Reference

Required Reading

Refer to Chapter 8 of the textbook:

- **Title:** *Operating System Concepts*
- **Authors:** Abraham Silberschatz, Peter Baer Galvin, and Greg Gagne
- **Publisher:** John Wiley & Sons
- **Edition:** 10th Edition (2018)



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Deadlocks Definition

Deadlock

- A **deadlock** is a situation in which a **set of processes are blocked** because each process is **holding** a resource and **waiting** for another resource acquired by some other process.
- In a deadlock state, no process can proceed because each is waiting for an event that can only be caused by another waiting process.

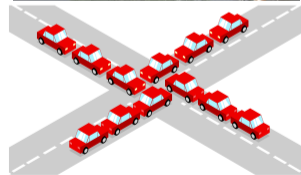


Figure 1: Deadlock Illustration



Real-World Deadlock Example

Database Transaction Deadlock

Two transactions accessing bank accounts:

Transaction T1

1. Lock Account A
2. Wait for Account B
3. Transfer \$100 from A to B
4. Release locks

Transaction T2

1. Lock Account B
2. Wait for Account A
3. Transfer \$50 from B to A
4. Release locks

⇒ **Result:** T1 holds A and waits for B, T2 holds B and waits for A

⇒ **Deadlock! Neither can proceed.**



System Model

System Model

A system consists of:

- **Processes:** P_1, P_2, \dots, P_n
 - **Resource Types:** R_1, R_2, \dots, R_m
- **Resource types:** R_1, R_2, \dots, R_m , e.g., CPU cycles, memory space, I/O devices, Files, database records, semaphores, etc.
 - **Each resource type R_i has W_i instances**, e.g., multiple CPUs, multiple I/O devices
 - Each process utilizes a resource as follows:
 1. **Request:** Process requests the resource type. If request cannot be granted, process must **wait**
 2. **Use:** Process operates on the resource
 3. **Release:** Process releases the resource

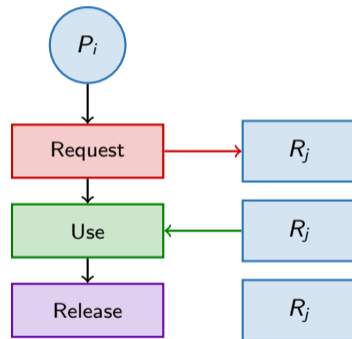


Figure 2: Process Resource Utilization

Necessary Conditions for Deadlock

Four Necessary Conditions

Deadlock can arise if **ALL FOUR** conditions hold **simultaneously**. These conditions are **not independent**, but are necessary:

1. Mutual Exclusion

- At least one resource must be held in a **non-sharable mode**
- Only one process can use the resource at a time

2. Hold and Wait

- At least one process must be **holding** one resource and **waiting** to acquire additional resources held by other processes

3. No Preemption

- Resources cannot be **forcibly taken** from a process
- Only released **voluntarily** by the holding process

4. Circular Wait

- Set $\{P_0, P_1, \dots, P_n\}$ where:
- P_0 waits for resource held by P_1 , P_1 waits for resource held by P_2 , ..., P_n waits for resource held by P_0

⇒ **Important:** All four conditions must hold **simultaneously**. **Breaking any one prevents deadlock.**



Illustrating the Four Conditions

Example: Communication ports

System has two Communication Ports and two processes: P_1 and P_2

Timeline of Events

1. P_1 requests and gets communication port 1
2. P_2 requests and gets communication port 2
3. P_1 requests communication port 2 (blocked)
4. P_2 requests communication port 1 (blocked)

Four Conditions Met

- **Mutual Exclusion:** Only one process per port, i.e. non-sharable ports
- **Hold and Wait:** P_1 holds port 1, waits for port 2
- **No Preemption:** Cannot force release
- **Circular Wait:** P_1 waits for port 2 held by P_2 ; P_2 waits for port 1 held by P_1

⇒ **Result: DEADLOCK!**



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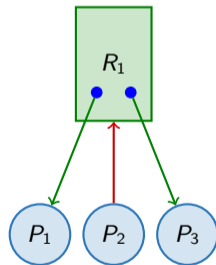
Resource Allocation Graph (RAG)

Resource Allocation Graph

A system can be described by a **Resource Allocation Graph (RAG)**: a **directed graph** with **two types of vertices (node) sets** (P and R) and **two types of edges** (**request** and **assignment**).

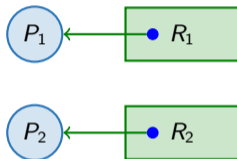
RAG Components

- **Vertices:**
 - $P = \{P_1, \dots, P_n\}$: **Processes (circles)**
 - $R = \{R_1, \dots, R_m\}$: **Resources (rectangles)**. Each resource type R_j has W_j instances (dots inside rectangle)
 - **Edges:**
 - **Request:** $P_i \rightarrow R_j$ (process requests resource)
 - **Assignment:** $R_j \rightarrow P_i$ (resource instance allocated to process)
- ⇒ **Deadlocks can be analyzed using RAGs!** (see next slides)



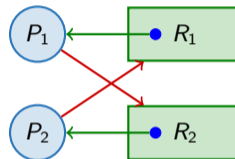
Deadlock Analysis Using RAG

No Cycle - No Deadlock



No cycle \Rightarrow No deadlock

Cycle - Deadlock



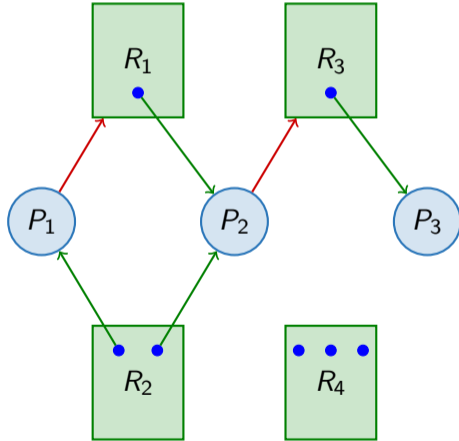
Cycle \Rightarrow Deadlock!

RAG Theorems (Basic Facts)

- No cycles \Rightarrow **No deadlock**
- Cycle + single instance per resource \Rightarrow **Deadlock**
- Cycle + multiple instances \Rightarrow **Possible deadlock**



RAG Example 1: No Deadlock

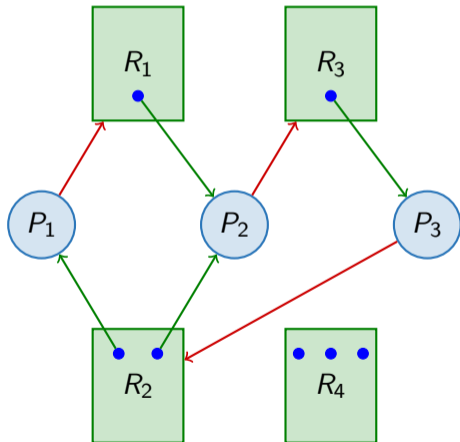


Analysis

- P_1 holds instance from R_2 , requests $R_1 \Rightarrow$ **Waiting** state
 - P_2 holds instances from R_1 and R_2 , requests $R_3 \Rightarrow$ **Waiting** state
 - P_3 holds instance from $R_3 \Rightarrow$ **Running/Ready** state
 - **No cycle exists**
- \Rightarrow **No Deadlock!** All processes can complete.



RAG Example 2: Deadlock Exists



Analysis

- P_1 holds instance from R_2 , requests $R_1 \Rightarrow$ **Waiting** state
- P_2 holds instances from R_1 and R_2 , requests $R_3 \Rightarrow$ **Waiting** state
- P_3 holds instance from R_3 , requests $R_2 \Rightarrow$ **Waiting** state

- **Two embedded cycles exist:**

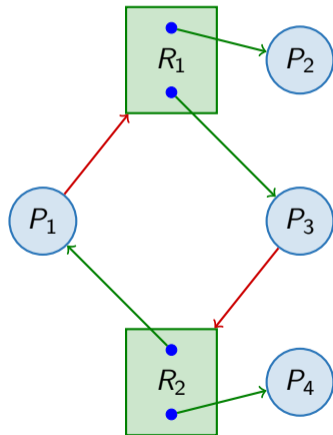
- $P_1 \rightarrow R_1 \rightarrow P_2 \rightarrow R_3 \rightarrow P_3 \rightarrow R_2 \rightarrow P_1$
- $P_2 \rightarrow R_3 \rightarrow P_3 \rightarrow R_2 \rightarrow P_2$

\Rightarrow **Deadlock Exists!** None can complete.

\Rightarrow **Deadlock despite multiple instances of R_2 ! All instances are held.**



RAG Example 3: Cycle but No Deadlock



Analysis

- P_1 holds instance from R_2 , requests $R_1 \Rightarrow$ **Waiting** state
 - P_2 holds instance from $R_1 \Rightarrow$ **Running/Ready** state
 - P_3 holds instance from R_1 , requests $R_2 \Rightarrow$ **Waiting** state
 - P_4 holds instance from $R_2 \Rightarrow$ **Running/Ready** state
 - **Cycle exists:**
 - $P_1 \rightarrow R_1 \rightarrow P_3 \rightarrow R_2 \rightarrow P_1$
- \Rightarrow **No Deadlock!** P_2 and P_4 can complete, releasing resources for P_1 and P_3 .



Key Takeaways

Key Takeaways

- **Deadlocks occur** when four necessary conditions hold simultaneously: **Mutual Exclusion, Hold and Wait, No Preemption, and Circular Wait.**
- A **Resource Allocation Graph (RAG)** models the state of resource allocation in a system using **processes** and **resources** vertices, and **request/assignment** edges.
- Deadlock analysis using RAGs:
 - **No cycles** in RAG \Rightarrow **No deadlock**
 - **Cycle + single instance per resource** \Rightarrow **Deadlock**
 - **Cycle + multiple instances** \Rightarrow **Possible deadlock**



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Strategies for Handling Deadlocks

Key Strategies

Three main strategies to handle deadlocks:

- **Ignore** the problem altogether and **pretend** deadlocks never occur in the system (*no mechanism for this strategy*)
- Use a protocol to **prevent** or **avoid** deadlocks from occurring (**prevention and avoidance methods discussed in next sections**)
- **Allow** deadlocks to occur, **detect** them, and **recover** from them (**detection and recovery methods discussed in later sections**)



Methods for Handling Deadlocks

Three Main Approaches

1. Deadlock Prevention

- Ensure at least **one of the four conditions** cannot hold
- Prevent deadlock from ever occurring
- May reduce resource utilization

2. Deadlock Avoidance

- Requires **advance information** about resource requests
- System decides whether to grant or delay requests
- Uses **Banker's Algorithm**

3. Detection and Recovery

- Allow deadlocks to occur
- **Detect** when deadlock happens (using **Wait-For Graphs** or **Banker's-like algorithms**)
- **Recover** from deadlock

⇒ **Trade-offs:** Each method has different costs, complexity, and performance implications.



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Deadlock Prevention

Prevention Strategy

Ensure **at least one of the four necessary conditions cannot hold** to **prevent** deadlocks from occurring.

1. Breaking "**Mutual Exclusion**" (Mutual Inclusion)
 - Some resources are **shareable** (e.g., read-only files, printers with spooling)
 - **Disadvantage**: Not always possible
2. Breaking "**Hold and Wait**"
 - **Protocol 1**: Request all resources at once
 - **Protocol 2**: Release all before requesting new ones
 - **Disadvantage**: Low utilization, starvation
3. Breaking "**No Preemption**"
 - If request fails, release all held resources
 - **Disadvantage**: Not always possible (e.g., printers, tapes)
4. **Circular Wait**
 - Impose total ordering: R_1, R_2, \dots, R_m
 - Request resources in **increasing order**
 - **Disadvantage**: May be difficult to define ordering



Prevention Example: Resource Ordering

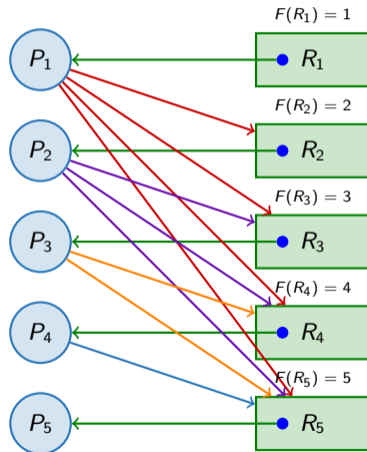
Breaking Circular Wait

Resource Ordering Strategy

- Assign a unique integer $F(R_j)$ to each resource type R_j in order to define a hierarchical ordering.
- Processes P_i holding resource instance R_j can request resource instance R_k only if $F(R_j) > F(R_k)$.

⇒ **Deadlock cannot occur as circular wait is prevented!**

Note: The ordering integer $F(R_j)$ can be assigned according to the demand rate history of resource R_j (lower demand → lower $F(R_j)$).



Key Takeaways

Key Takeaways

- **Deadlock Prevention** ensures that at least one of the four necessary conditions for deadlock cannot hold, effectively preventing deadlocks from occurring.
- Methods to break each condition:
 - **Mutual Exclusion**: Make resources shareable when possible.
 - **Hold and Wait**: Require processes to request all resources at once or release held resources before requesting new ones.
 - **No Preemption**: Allow preemption of resources when requests cannot be granted.
 - **Circular Wait**: Impose a total ordering on resource types and require processes to request resources in increasing order.
- ⇒ **Trade-offs**: While prevention methods can effectively eliminate deadlocks, they may lead to reduced resource utilization and increased complexity in resource management.



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Deadlock Avoidance: Overview

Avoidance Approach

Requires that the system has some **additional a priori information** available

Key Requirements

- **Simplest model**: Each process declares the **maximum number** of resources of each type that it may need
- The deadlock-avoidance algorithm **dynamically examines** the resource-allocation state
- Ensures that there can never be a **circular-wait condition**
- **Resource-allocation state** defined by:
 - **Number of available and allocated resources**
 - **Maximum demands of the processes**

Two Algorithms

1. **Resource-Allocation Graph Algorithm**: For single instance per resource type
2. **Banker's Algorithm**: For multiple instances per resource type



Safe State Definition

Safe State

System is in a **safe state** if there exists a **safe sequence** $\langle P_1, P_2, \dots, P_n \rangle$ of **ALL** processes such that for each P_i , the resources that P_i can still request can be satisfied by **currently available resources** + **resources held by all P_j with $j < i$** .

Safe Sequence Properties

- If P_i resource needs are not immediately available, then P_i can **wait** until all P_j ($j < i$) have finished
 - When P_j finishes, P_i can **obtain needed resources**, **execute**, **return allocated resources**, and **terminate**
 - When P_i terminates, P_{i+1} can obtain its needed resources, and so on...
- ⇒ **Important:** If no such sequence exists, the system is in an **unsafe state**.



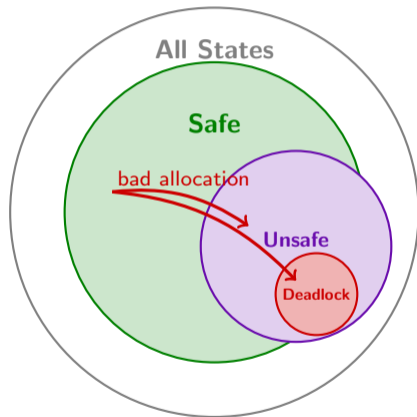
Safe vs. Unsafe vs. Deadlock States

Basic Facts

- Safe state \Rightarrow **No deadlock**
- Unsafe state \Rightarrow **Possibility of deadlock**
- Deadlock state \Rightarrow **Deadlock**

Avoidance Strategy

- **Ensure** that the system will **never enter** an **unsafe state**
- When a process requests a resource, **ask**: *"If we grant this request, will the system remain in a safe state?"*
 - If yes \Rightarrow **Grant**
 - If no \Rightarrow **Deny/Delay**



Goal: Stay in safe region!



Safe State: Illustration Example

System with 12 Resources

3 processes: P_0, P_1, P_2 ; Total: 12 resource instances

At time t_0

Process	Max	Allocated	Need
P_0	10	5	5
P_1	4	2	2
P_2	9	2	7
Available			3

- P_1 : needs ≤ 2 (available: 3) ✓
- P_0 : needs ≤ 5 (available: 5) ✓
- P_2 : needs ≤ 7 (available: 10) ✓

Safe sequence: $\langle P_1, P_0, P_2 \rangle$

⇒ Safe state!

At time t_1 : P_2 requests 1 more

Process	Max	Current	Need
P_0	10	5	5
P_1	4	2	2
P_2	9	3	6
Available			2

Analysis:

- Only P_1 can complete (needs ≤ 2)
- After P_1 : Available = 4
- P_0 needs 5 (cannot satisfy!)
- P_2 needs 6 (cannot satisfy!)

⇒ Unsafe state!



RAG Algorithm for Avoidance

For Single Instance per Resource Type

Use Resource-Allocation Graph with **Claim Edges**

New Edge Type

- **Claim edge** $P_i \dashrightarrow R_j$: Process P_i **may request** resource R_j in the future (represented by **dashed line**)
- **Claim edge** converts to **request edge** when process requests the resource
- **Request edge** converts to **assignment edge** when resource is allocated
- **Assignment edge** reconverts to **claim edge** when resource is released

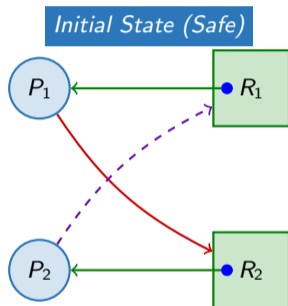
Safety Check Algorithm

Suppose process P_i requests resource R_j :

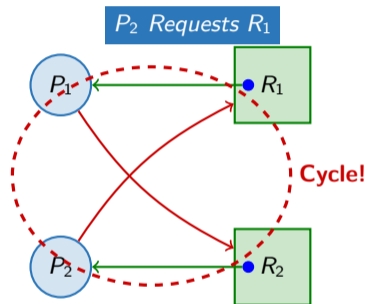
- Request can be granted **only if** converting the **claim edge** $P_i \dashrightarrow R_j$ to a **request edge** $P_i \rightarrow R_j$ **does not create a cycle** in the RAG
- If cycle would form \Rightarrow **Deny request** (unsafe state)



RAG Avoidance: Example



P_1 holds R_1 , requests R_2
 P_2 holds R_2 , may claim R_1
 \Rightarrow **Safe state (no cycle)**



Claim \dashrightarrow Request: Forms cycle!
Cycle: $P_2 \rightarrow R_1 \rightarrow P_1 \rightarrow R_2 \rightarrow P_2$
 \Rightarrow **Deny request**

\Rightarrow **Decision:** System **denies** P_2 's request for R_1 to avoid entering unsafe state



Banker's Algorithm: Overview

For Multiple Instances per Resource Type

Use **Banker's Algorithm** to ensure system remains in **safe state**. It follows the principle of banking: *never allocate resources that may not be available in the future.*

Requirements

- Each process must **a priori claim** maximum use
- When a process requests a resource, it may have to **wait**
- When a process gets all its resources, it must **return them in finite time**

Data Structures (Let $n = \#$ processes, $m = \#$ resource types)

- **Available** $[m]$: Array of length m . $\text{Available}[j] = k$ means k instances of R_j available
- **Max** $[n][m]$: $n \times m$ matrix. $\text{Max}[i][j] = k$ means P_i may request at most k instances of R_j
- **Allocation** $[n][m]$: $n \times m$ matrix. $\text{Allocation}[i][j] = k$ means P_i currently holds k instances of R_j
- **Need** $[n][m]$: $n \times m$ matrix. $\text{Need}[i][j] = k$ means P_i may need k more instances of R_j

$$\text{Need}[i][j] = \text{Max}[i][j] - \text{Allocation}[i][j]$$



Banker's Algorithm: Safety Algorithm

Algorithm 1: Safety Algorithm - Check if system is in safe state

Input: n processes, m resource types, Available, Allocation, Need matrices

Output: Determine if system is in safe state (SAFE or UNSAFE)

// Step 1: Initialize

```
1 Let Work and Finish be vectors of length  $m$  and  $n$ 
2  $Work[j] \leftarrow Available[j]$  for all  $j \in \{0, \dots, m-1\}$ 
3  $Finish[i] \leftarrow \text{false}$  for all  $i \in \{0, \dots, n-1\}$ 
// Step 2: Find process that can finish
4 repeat
5   Find index  $i \in \{0, \dots, n-1\}$  such that:
6     (a)  $Finish[i] == \text{false}$ 
7     (b)  $Need[i][j] \leq Work[j]$  for all  $j \in \{0, \dots, m-1\}$ 
8   if such  $i$  exists then
9     // Step 3: Simulate allocation
10     $Work[j] \leftarrow Work[j] + Allocation[i][j]$  for all  $j \in \{0, \dots, m-1\}$ 
11     $Finish[i] \leftarrow \text{true}$ 
12  end
13 until no such  $i$  exists;
// Step 4: Check if all processes can finish
14 if  $Finish[i] == \text{true}$  for all  $i \in \{0, \dots, n-1\}$  then
15   return SAFE
16 else
17   return UNSAFE
18 end
```



Banker's Algorithm: Example Setup

System with 5 Processes and 3 Resource Types

Resource Types: A (10 instances), B (5 instances), C (7 instances)

Snapshot at time T_0

	Max			Allocation			Need		
	A	B	C	A	B	C	A	B	C
P_0	7	5	3	0	1	0	7	4	3
P_1	3	2	2	2	0	0	1	2	2
P_2	9	0	2	3	0	2	6	0	0
P_3	2	2	2	2	1	1	0	1	1
P_4	4	3	3	0	0	2	4	3	1

Available		
A	B	C
3	3	2

Resource Summary

- **Need = Max - Allocation**
- **Total resources:** A = 10, B = 5, C = 7
- **Allocated resources:**
 - A: $0 + 2 + 3 + 2 + 0 = 7$
 - B: $1 + 0 + 0 + 1 + 0 = 2$
 - C: $0 + 0 + 2 + 1 + 2 = 5$
- **Available resources:**
 - A: $10 - 7 = 3$
 - B: $5 - 2 = 3$
 - C: $7 - 5 = 2$



Banker's Algorithm: Safety Check

Is the system in a safe state?

	Max			Allocation			Need		
	A	B	C	A	B	C	A	B	C
P_0	7	5	3	0	1	0	7	4	3
P_1	3	2	2	2	0	0	1	2	2
P_2	9	0	2	3	0	2	6	0	0
P_3	2	2	2	2	1	1	0	1	1
P_4	4	3	3	0	0	2	4	3	1

Apply Safety Algorithm

Initialize:

- Work = Available = (3,3,2)
- Finish[i] = false for all i = [F,F,F,F,F]

Iterations:

1. P_1 : Need = (1,2,2) \leq (3,3,2) \checkmark
 - Work = (3,3,2) + (2,0,0) = (5,3,2)
 - Finish[1] = true \rightarrow [F,T,F,F,F]
2. P_3 : Need = (0,1,1) \leq (5,3,2) \checkmark
 - Work = (5,3,2) + (2,1,1) = (7,4,3)
 - Finish[3] = true \rightarrow [F,T,F,T,F]

3. P_4 : Need = (4,3,1) \leq (7,4,3) \checkmark
 - Work = (7,4,3) + (0,0,2) = (7,4,5)
 - Finish[4] = true \rightarrow [F,T,F,T,T]
4. P_2 : Need = (6,0,0) \leq (7,4,5) \checkmark
 - Work = (7,4,5) + (3,0,2) = (10,4,7)
 - Finish[2] = true \rightarrow [F,T,T,T,T]
5. P_0 : Need = (7,4,3) \leq (10,4,7) \checkmark
 - Work = (10,4,7) + (0,1,0) = (10,5,7)
 - Finish[0] = true \rightarrow [T,T,T,T,T]

\Rightarrow **Result:** All Finish[i] = true

Safe sequence: $\langle P_1, P_3, P_4, P_2, P_0 \rangle$

System is in **SAFE state!**



Banker's Algorithm: Resource-Request Algorithm

Algorithm 2: Resource-Request Algorithm - Process P_i requests resources

Input: Request[i] = request vector for process P_i of length m

Output: Grant or deny the request

// Step 1: Check if request exceeds maximum claim

```
1 if Request[i][j] > Need[i][j] for any  $j \in \{0, \dots, m-1\}$  then
2   | raise error (exceeded maximum claim)
3 end
```

// Step 2: Check if resources are available

```
4 if Request[i][j] > Available[j] for any  $j \in \{0, \dots, m-1\}$  then
5   |  $P_i$  must WAIT (resources not available)
6 end
```

// Step 3: Pretend to allocate

```
7 Available[j] ← Available[j] - Request[i][j] for all  $j \in \{0, \dots, m-1\}$ 
8 Allocation[i][j] ← Allocation[i][j] + Request[i][j] for all  $j \in \{0, \dots, m-1\}$ 
9 Need[i][j] ← Need[i][j] - Request[i][j] for all  $j \in \{0, \dots, m-1\}$ 
```

// Step 4: Run safety algorithm (see Algorithm 1)

```
10 if system is in safe state then
11   | GRANT resources to  $P_i$  (keep changes)
12 else
13   | DENY request,  $P_i$  must WAIT or ROLLBACK
14   | Restore old state (undo changes)
15 end
```



Banker's Algorithm: Request Example 1

P_1 requests (1, 0, 2)

Step 1: Check against Need

- Request₁ = (1,0,2), Need₁ = (1,2,2)
- Request₁ ≤ Need₁? **YES ✓**

Step 2: Check against Available

- Request₁ = (1,0,2), Available = (3,3,2)
- Request₁ ≤ Available? **YES ✓**

Step 3: Pretend to allocate

	Max			Allocation			Need		
	A	B	C	A	B	C	A	B	C
P_0	7	5	3	0	1	0	7	4	3
P_1	3	2	2	3	0	2	0	2	0
P_2	9	0	2	3	0	2	6	0	0
P_3	2	2	2	2	1	1	0	1	1
P_4	4	3	3	0	0	2	4	3	1

Available		
A	B	C
2	3	0

Step 4: Run Safety Algorithm

Work = Available = (2,3,0)

- P_1 : Need = (0,2,0) ≤ (2,3,0) ✓ ⇒ Work = (5,3,2)
- P_3 : Need = (0,1,1) ≤ (5,3,2) ✓ ⇒ Work = (7,4,3)
- P_4 : Need = (4,3,1) ≤ (7,4,3) ✓ ⇒ Work = (7,4,5)
- P_0 : Need = (7,4,3) ≤ (7,4,5) ✓ ⇒ Work = (7,5,5)
- P_2 : Need = (6,0,0) ≤ (7,5,5) ✓ ⇒ Work = (10,5,7)

⇒ **Decision: Safe sequence** $\langle P_1, P_3, P_4, P_0, P_2 \rangle$ exists
 System remains in **SAFE state**

GRANT the request to P_1



Banker's Algorithm: Request Example 2

P_4 requests (3, 3, 0) - Apply on the original state

Step 1: Check against Need

- Request₄ = (3,3,0), Need₄ = (4,3,1)
- Request₄ ≤ Need₄? **YES ✓**

Step 2: Check against Available

- Request₄ = (3,3,0), Available = (3,3,2)
- Request₄ ≤ Available? **YES ✓**

Step 3: Pretend to allocate

	Max			Allocation			Need		
	A	B	C	A	B	C	A	B	C
P_0	7	5	3	0	1	0	7	4	3
P_1	3	2	2	2	0	0	1	2	2
P_2	9	0	2	3	0	2	6	0	0
P_3	2	2	2	2	1	1	0	1	1
P_4	4	3	3	3	3	2	1	0	1

Available		
A	B	C
0	0	2

Step 4: Run Safety Algorithm

Work = Available = (0,0,2)

Check all processes:

- P_0 : Need = (7,4,3) $\not\leq$ (0,0,2) **NO**
- P_1 : Need = (1,2,2) $\not\leq$ (0,0,2) **NO**
- P_2 : Need = (6,0,0) $\not\leq$ (0,0,2) **NO**
- P_3 : Need = (0,1,1) $\not\leq$ (0,0,2) **NO**
- P_4 : Need = (1,0,1) $\not\leq$ (0,0,2) **NO**

No process can proceed!

⇒ **Decision: No safe sequence exists**
 System would be in **UNSAFE state**

DENY the request to P_4



Banker's Algorithm: Request Example 3

P_0 requests (0, 2, 0) - Apply on the original state

Step 1: Check against Need

- Request₀ = (0,2,0), Need₀ = (7,4,3)
- Request₀ ≤ Need₀? **YES ✓**

Step 2: Check against Available

- Request₀ = (0,2,0), Available = (3,3,2)
- Request₀ ≤ Available? **YES ✓**

Step 3: Pretend to allocate

	Max			Allocation			Need		
	A	B	C	A	B	C	A	B	C
P_0	7	5	3	0	3	0	7	2	3
P_1	3	2	2	2	0	0	1	2	2
P_2	9	0	2	3	0	2	6	0	0
P_3	2	2	2	2	1	1	0	1	1
P_4	4	3	3	0	0	2	4	3	1

Available		
A	B	C
3	1	2

Step 4: Run Safety Algorithm

Work = Available = (3,1,2)

- P_3 : Need = (0,1,1) ≤ (3,1,2) ✓ ⇒ Work = (5,2,3)
- P_1 : Need = (1,2,2) ≤ (5,2,3) ✓ ⇒ Work = (7,2,3)
- P_0 : Need = (7,2,3) ≤ (7,2,3) ✓ ⇒ Work = (7,5,3)
- P_4 : Need = (4,3,1) ≤ (7,5,3) ✓ ⇒ Work = (7,5,5)
- P_2 : Need = (6,0,0) ≤ (7,5,5) ✓ ⇒ Work = (10,5,7)

⇒ **Decision:** Safe sequence $\langle P_3, P_1, P_0, P_4, P_2 \rangle$ exists
 System remains in **SAFE state**

GRANT the request to P_0



Key Takeaways

Key Takeaways

- **Deadlock avoidance** ensures that system will never enter an unsafe state by **dynamically** examining resource-allocation state to ensure that there can never be a circular-wait condition.
- The **Banker's Algorithm** is a deadlock-avoidance algorithm that tests for safety by simulating the allocation of predetermined maximum possible amounts of all resources, and then makes an "s-state" check to test for possible deadlock conditions for all other pending activities, before deciding whether allocation should be allowed to continue.
- The **safety algorithm** is used to determine whether a system is in a safe state or an unsafe state.
- When a process makes a request for resources, the **Banker's Algorithm** determines whether the request can be granted immediately or must be delayed until it is safe to do so.



Outline

1. Introduction to Deadlocks
2. Resource-Allocation Graph
3. Methods for Handling Deadlocks
4. Deadlock Prevention
5. Deadlock Avoidance
6. Deadlock Detection and Recovery
 - 6.1 Detection for Single Instance (Wait-For Graph)
 - 6.2 Detection for Multiple Instances (Banker's-like Algorithm)
 - 6.3 Recovery from Deadlock
 - 6.4 Key Takeaways

Allow-Detection-Recovery Approach: Overview

Allow-Detect-Recover Strategy

If system does **not** employ **prevention** or **avoidance** techniques, then it **must** have mechanism that **allows** system to enter **deadlock state**, provides algorithm to **detect** deadlock, and provides algorithm to **recover** from deadlock.

Key Questions

1. **When to invoke** detection algorithm?
 - Depends on how often deadlocks occur
 - Depends on how many processes affected
2. **Which algorithm** to use?
 - Single instance: **Wait-for Graph**
 - Multiple instances: **Detection Algorithm** (similar to Banker's)
3. **How to recover?**
 - Process termination
 - Resource preemption



Detection Algorithm: Single Instance per Resource Type

Wait-For Graph Construction

- **Nodes:** Processes only (no resource nodes)
- **Edge** $P_i \rightarrow P_j$: Process P_i is **waiting for** process P_j to release a resource
- **Conversion from RAG to Wait-for graph consists:**
 - If P_i holds resource R and P_j requests R , create edge $P_j \rightarrow P_i$
 - If multiple resources held/requested, create multiple edges

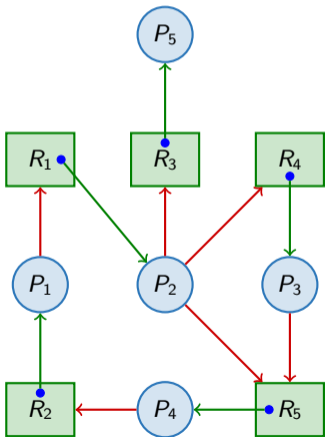
Detection Algorithm

- Periodically invoke algorithm that searches for **cycle**
- If cycle exists \Rightarrow **Deadlock!**
- Algorithm requires $O(n^2)$ operations, where n = number of vertices (processes)
- **Reducing RAG to Wait-for graph reduce complexity of cycle detection from $O(m + n)$ to $O(n^2)$, where m = number of edges**

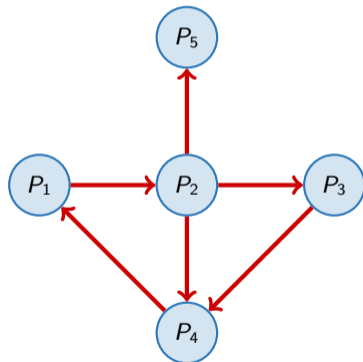


Wait-For Graph: Example

Resource Allocation Graph



Wait-For Graph



⇒ 2 cycles can be easily detected here!



Detection Algorithm: Multiple Instances per Resource Type

Principle

For multiple instances per resource type: use an algorithm similar to Banker's Algorithm to **detect** if system is in **deadlock state** but **without** making use of **Max** and **Need** matrices. Use only **Allocation** and **Request** matrices.

Data Structures (Let $n = \#$ processes, $m = \#$ resource types)

- **Available**[m]: Number of available resources of each type
- **Allocation**[n][m]: Resources currently allocated to each process
- **Request**[n][m]: Current request of each process
 - Request[i][j] = k means P_i is requesting k more instances of R_j

⇒ **Key Difference from Banker's**: Uses **Request** (current requests) instead of **Need** (maximum future needs)



Detection Algorithm: Multiple Instances per Resource Type

Algorithm 3: Detection Algorithm - Banker's-like for Multiple Instances

Input: n processes, m resource types, Available, Allocation, Request matrices

Output: Determine if deadlock exists and identify deadlocked processes

// Step 1: Initialize

- 1 Let **Work** and **Finish** be vectors of length m and n
- 2 $Work[j] \leftarrow Available[j]$ for all $j \in \{0, 1, \dots, m - 1\}$
- 3 $Finish[i] \leftarrow$ **false** (if $Allocation[i] \neq 0$) **true** (if $Allocation[i] = 0$) for all $i \in \{0, 1, \dots, n - 1\}$

// Step 2: Find process whose request can be satisfied

- 4 **repeat**
- 5 Find index i such that:
 - 6 (a) $Finish[i] ==$ **false**
 - 7 (b) $Request[i][j] \leq Work[j]$ for all $j \in \{0, 1, \dots, m - 1\}$
- 8 **if** such i exists **then**
 - 9 // Step 3: Simulate release
 - 9 $Work[j] \leftarrow Work[j] + Allocation[i][j]$ for all $j \in \{0, 1, \dots, m - 1\}$
 - 10 $Finish[i] \leftarrow$ **true**
- 11 **end**
- 12 **until** no such i exists;
- 13 // Step 4: Check for deadlock
- 13 **if** $Finish[i] ==$ **false** for some i **then**
 - 14 **return** **DEADLOCK exists**
 - 15 **Deadlocked processes:** all P_i where $Finish[i] ==$ **false**
- 16 **else**
 - 17 **return** **NO DEADLOCK**
- 18 **end**



Detection Algorithm: Example 1 (No Deadlock)

5 processes, 3 resource types

Resources Types: A (7 instances), B (2 instances), C (6 instances)

Snapshot at time T_0

	Allocation			Request		
	A	B	C	A	B	C
P_0	0	1	0	0	0	0
P_1	2	0	0	2	0	2
P_2	3	0	3	0	0	0
P_3	2	1	1	1	0	0
P_4	0	0	2	0	0	2
Available	0	0	0			

Note: Total resources = (7,2,6), Allocated = (7,2,6), Available = (0,0,0)

Step 1: Initialize

- Work = Available = (0,0,0)
- Finish = [F, F, F, F, F] (all hold resources)

Step 2-3: Find processes that can complete

1. P_0 : Request = (0,0,0) \leq (0,0,0) ✓
 - Work = (0,0,0) + (0,1,0) = **(0,1,0)**
 - Finish[P_0] = true \rightarrow [T, F, F, F, F]
2. P_2 : Request = (0,0,0) \leq (0,1,0) ✓
 - Work = (0,1,0) + (3,0,3) = **(3,1,3)**
 - Finish[P_2] = true \rightarrow [T, F, T, F, F]
3. P_3 : Request = (1,0,0) \leq (3,1,3) ✓
 - Work = (3,1,3) + (2,1,1) = **(5,2,4)**
 - Finish[P_3] = true \rightarrow [T, F, T, T, F]



Detection Algorithm: Example 1 (Contd.)

5 processes, 3 resource types (Contd.)

4. P_1 : Request = $(2,0,2) \leq (5,2,4)$ ✓
 - Work = $(5,2,4) + (2,0,0) = (7,2,4)$
 - Finish[P_1] = true → [T, T, T, T, F]
5. P_4 : Request = $(0,0,2) \leq (7,2,4)$ ✓
 - Work = $(7,2,4) + (0,0,2) = (7,2,6)$
 - Finish[P_4] = true → [T, T, T, T, T]

Step 4: Check for deadlock

- All Finish[i] = true for all $i \in \{0, 1, 2, 3, 4\}$
- Sequence: $\langle P_0, P_2, P_3, P_1, P_4 \rangle$

⇒ **Result: NO DEADLOCK**

All processes can complete successfully



Detection Algorithm: Example 2 (With Deadlock)

Same system, P_2 requests additional instance of C

Modified Request Matrix

	Allocation			Request		
	A	B	C	A	B	C
P_0	0	1	0	0	0	0
P_1	2	0	0	2	0	2
P_2	3	0	3	0	0	1
P_3	2	1	1	1	0	0
P_4	0	0	2	0	0	2
Available				0	0	0

Apply Detection Algorithm

- Work = (0,0,0)
- P_0 : Request = (0,0,0) $\checkmark \Rightarrow$ Work = (0,1,0)
- P_2 : Request = (0,0,1) \leq (0,1,0)? **NO!**
- P_3 : Request = (1,0,0) \leq (0,1,0)? **NO!**
- P_1, P_4 : Cannot satisfy requests

Final State

- Finish = [true, false, false, false, false]
- Can only reclaim resources from P_0
- Insufficient resources to fulfill other processes' requests

Result: DEADLOCK EXISTS!

Deadlocked processes: P_1, P_2, P_3, P_4

These processes form one or more **disjoint cycles**

Observations

- Single additional request by P_2 caused deadlock
- Four out of five processes are deadlocked
- Recovery mechanism must now be invoked



Detection Algorithm Usage

When to Invoke Detection Algorithm? Decision depends on two factors:

1. How Often Deadlocks Occur

- If deadlocks occur **frequently** \Rightarrow invoke detection **frequently**
- If deadlocks occur **rarely** \Rightarrow invoke detection **less often**

2. How Many Processes Affected

- More cycles \Rightarrow More processes affected
- Difficult to identify which process "**caused**" the deadlock

Invocation Strategies

1. **Every resource request**: High overhead, but can identify cause (culprit) easily
2. **Fixed time intervals**: Reasonable overhead
3. **CPU utilization drops**: When system appears idle

\Rightarrow **Trade-off**: More frequent detection = Higher overhead BUT easier to identify cause



Recovery: Overview

Once deadlock is detected, system must **break** the deadlock. Two main approaches exist:

1. Process Termination

- Kill one or more processes
- Free their resources
- Simple to implement
- **Problem**: Lose work done

2. Resource Preemption

- Take resources from processes
- Give to other processes
- May require rollback
- **Problem**: Starvation risk



Process Termination

Method 1: Abort All Deadlocked Processes

- **Advantage:** Simple, definitely breaks deadlock
- **Disadvantage:** Very expensive - all partial computations lost

Method 2: Abort One Process at a Time

- Kill one process
- Run detection algorithm again
- Repeat until deadlock is eliminated
- **Advantage:** Less waste
- **Disadvantage:** High overhead (repeated detection)

Selection Criteria: Which Process to Terminate?

1. **Priority** of the process
2. **Computation time** and remaining time to completion
3. **Resources** used and needed
4. **Number of processes** that will need to be terminated



Resource Preemption

Successively **preempt** resources until deadlock is broken

Three Issues to Address

1. Selecting a Victim

- Which resources and processes to preempt?
- **Goal:** Minimize cost
- **Cost factors:** Number of resources held, execution time consumed

2. Rollback

- If preempt resource from process, what to do with process?
- **Total rollback:** Abort and restart process
- **Partial rollback:** Return to some **safe state**
- Requires system to maintain **checkpoint** information

3. Starvation

- Same process may always be picked as victim
- Process never completes its task
- **Solution:** Include **number of rollbacks** in cost factor



Recovery Situation Analysis

What is the situation?

- A deadlock has occurred involving multiple processes P_1, P_2, \dots, P_n
- None of the processes can continue because each is **waiting for resources held by others**
- The operating system must **recover** from deadlock

The situation is evaluated based on these metrics:

- **Priority** → how important each process is
- **Time** → percentage of work already completed by each process
- **Resources** → number of resources currently held by each process

⇒ **Tip:** Choose to terminate or preempt from the process that minimizes overall **cost based on these metrics**. In practice, this is often the process with **lowest priority, least progress made, and fewest resources held**.



Recovery: Example Scenario Analysis

Process Termination vs. Preemption

Deadlock: P_1, P_2, P_3, P_4 are deadlocked

Process Information

Process	Priority	Time	Resources
P_1	High	90%	3
P_2	Low	10%	2
P_3	Medium	50%	4
P_4	Medium	80%	2

Time = % completion

Decision Analysis

- **Terminate** P_1 : High priority, high progress lost
- **Terminate** P_3 : Medium priority, moderate progress lost
- **Terminate** P_4 : Medium priority, high progress lost
- **Terminate** P_2 : Low priority, minimal progress lost
- **Preempt from** P_1 : High priority, rollback significant progress
- **Preempt from** P_3 : Medium priority, rollback moderate progress
- **Preempt from** P_4 : Medium priority, rollback high progress
- **Preempt from** P_2 : Low priority, rollback minimal progress

⇒ **Best Strategy:** **Terminate or Preempt from** P_2



Key Takeaways

Key Takeaways

- **Deadlock detection** identifies deadlocks using Resource Allocation Graphs (Wait-For Graphs) for single instances or Banker's-like algorithm for multiple instances
- **Detection frequency** depends on how often deadlocks occur and how many processes are affected
- **Recovery** from deadlock involves either process termination or resource preemption
- **Process termination** can be done by aborting all deadlocked processes or one at a time
- **Resource preemption** requires selecting a victim, rolling back, and avoiding starvation



Outline

1. Introduction to Deadlocks
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7. Exercise

Exercise: System State Analysis

System State Analysis

Let's suppose the following snapshot of the system at a given moment. It contains:

- 5 processes P_0, P_1, P_2, P_3 and P_4
- 4 types of resources A, B, C and D with 12, n , 8 and m instances, respectively
- Matrices "Allocation" and "Max" that represent, for each process, the allocated instances from each resource type, and its maximum need, respectively

Questions:

1. Fill the vector "Available"
2. Fill the matrix "Need"
3. What are the two conditions (expressed by n , m , x and y), according to them, P_0 can be executed firstly then the system can be in a safe state?
4. What are the two conditions (expressed by n , m and x), according to them, P_4 can be executed firstly then the system can be in a safe state?

	Allocation				Max			
	A	B	C	D	A	B	C	D
P_0	2	0	0	1	4	2	1	y
P_1	3	1	2	1	7	2	5	2
P_2	2	1	0	3	6	3	1	6
P_3	1	3	1	2	5	4	2	4
P_4	1	x	3	2	3	6	5	5



Solution: (Questions a & b)

Calculating Available and CurrentNeed

a) Available vector:

Total resources - Allocated resources = Available

- Available[A] = $12 - (2+3+2+1+1) = 12 - 9 = 3$
- Available[B] = $n - (0+1+1+3+x) = n - (5+x) = n-5-x$
- Available[C] = $8 - (0+2+0+1+3) = 8 - 6 = 2$
- Available[D] = $m - (1+1+3+2+2) = m - 9 = m-9$

b) Need matrix: Need = Max - Allocation

	CurrentNeed			
	A	B	C	D
P_0	2	2	1	$y-1$
P_1	4	1	3	1
P_2	4	2	1	3
P_3	4	1	1	2
P_4	2	$6-x$	2	3



Solution: (Questions c & d)

Conditions for Safe State

c) For P_0 to execute first:

CurrentNeed[P_0] \leq Available

$$\bullet (2, 2, 1, y-1) \leq (3, n-5-x, 2, m-9)$$

This gives us:

1. $n-5-x \geq 2 \Rightarrow n \geq 7+x$
2. $m \geq y+8$

d) For P_4 to execute first:

CurrentNeed[P_4] \leq Available

$$\bullet (2, 6-x, 2, 3) \leq (3, n-5-x, 2, m-9)$$

This gives us:

1. $n-5-x \geq 6-x \Rightarrow n \geq 11$
2. $m \geq 12$



End of Chapter 6